

GW-Gamma-Rays Delay & Afterglow Polarization

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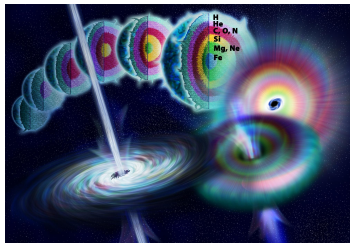


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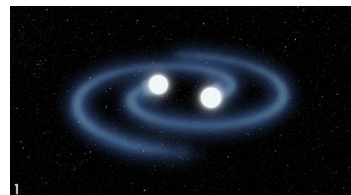
Feb 28, 2024

Gamma-ray burst progenitors as GW sources



Progenitors of **long-GRBs** ($T_{90} > 2$ s) are massive ($M \geq 20 - 30 M_{\odot}$) Wolf-Rayet stars that undergo core-collapse. (Woosley '93; Woosley & Bloom '06)

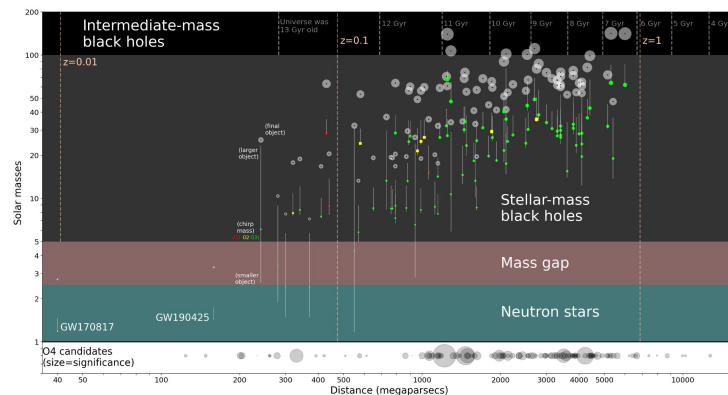
Short-GRBs ($T_{90} < 2$ s) are produced in the mergers of two NSs (e.g. [GW170817](#)) and NS + BH. (Eichler+89; Narayan+92)



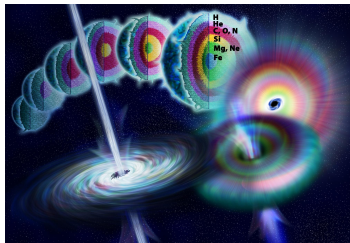
To lowest order, GWs are emitted when a rapidly changing mass distribution produces a **time-varying quadrupole moment**

GWs in the collapsar scenario

- Rotational instability in the central engine (Davies+02; Fryer+02; Kobayashi & Meszaros '03; Shibata+03; ...)
- Estimates are still uncertain
- GW-gamma-ray delay can be up to few x 10s due to longer breakout times (Bromberg+12)

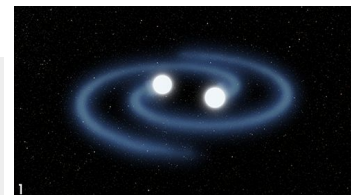


Gamma-ray burst progenitors as GW sources



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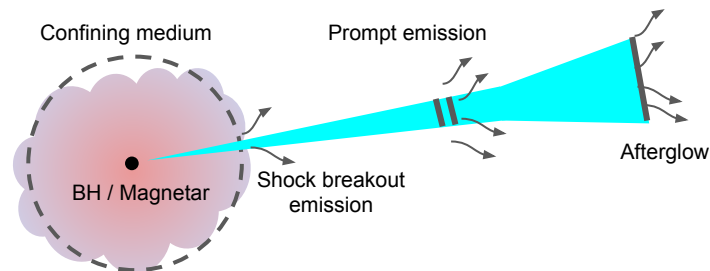
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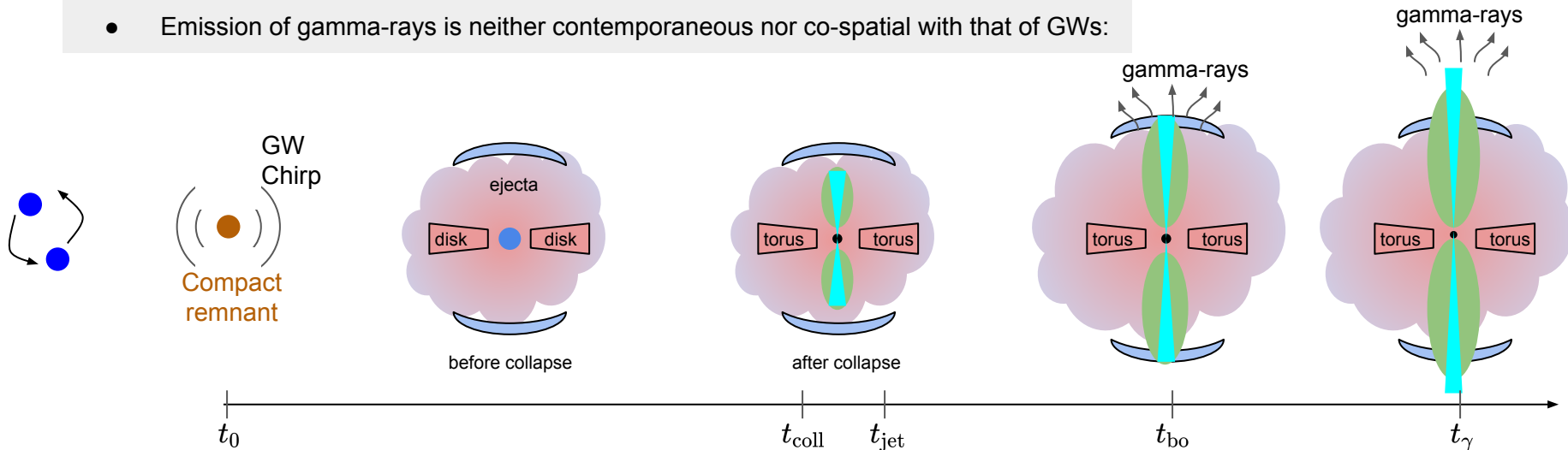
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Why a delay between GWs and gamma-rays?

- Emission of gamma-rays is neither contemporaneous nor co-spatial with that of GWs:



- Total delay w.r.t GW emission: $t_{\text{del}} = [t_{\text{coll}} + t_{\text{jet}} + t_{\text{bo}} + t_\gamma] (1 + z)$

- Gravitons and gamma-ray photons move at different speeds:

$$t_{\text{del}} = \frac{D}{c} \left(1 - \frac{c}{c_{\text{GW}}} \right) \longrightarrow \left(1 - \frac{c}{c_{\text{GW}}} \right) \simeq 4.2 \times 10^{-16} \left(\frac{D}{40 \text{ Mpc}} \right)^{-1} \left(\frac{t_{\text{del}}}{1.74 \text{ s}} \right)$$

This delay can also be used to constrain the **Shapiro delay** that tests the **weak-equivalence principle** (e.g. LIGO-VIRGO-Fermi-INTEGRAL '17)

Merger remnant and collapse time

Stable NS: Long-lived NS, rapidly spinning, possibly with magnetar strength B-fields ($B_s \sim 10^{14-15}$ G), that loses rotational energy due to magnetic dipole radiation on the spin-down time

$$\tau_{\text{sd}} = \frac{Ic^3}{2f\Omega_0 R_{\text{NS}}^6 B_0^2} \geq 3.4 \times 10^2 \frac{P_{0,-3}^2}{fB_{15}^2} \text{ s}$$

Supra-massive NS: Supported by rigid-body rotation; collapses to a BH on the spin-down time (if GW emission is sub-dominant):

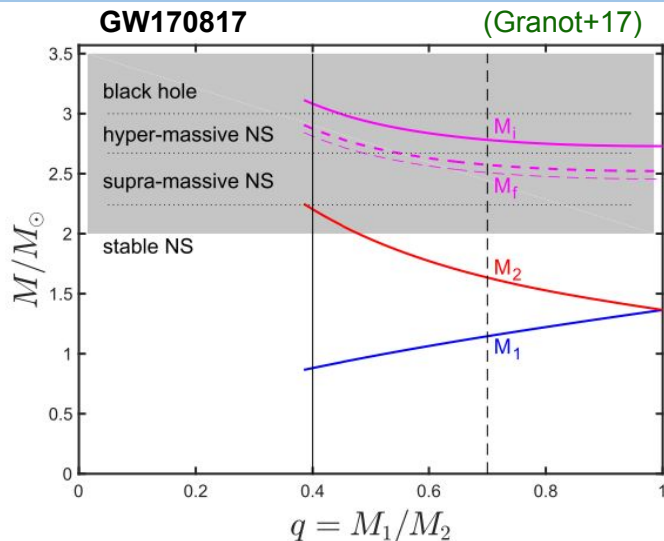
$$t_{\text{coll}} = \tau_{\text{sd}} \quad E_{\text{rot}} = \frac{1}{2} I \Omega_0^2 \sim 10^{52.5-53} \text{ erg}$$

Hyper-massive NS: Supported by differential rotation; collapses to a BH on a much shorter timescale: (e.g. Kastaun & Galeazzi '15)

$$10^{-2} \text{ s} \leq t_{\text{coll}} \leq 1 \text{ s}$$

Prompt BH: BH forms directly if $M_{\text{tot}} \geq 2.8M_{\odot}$; mass of ejected matter is less

$$t_{\text{coll}} = 0$$



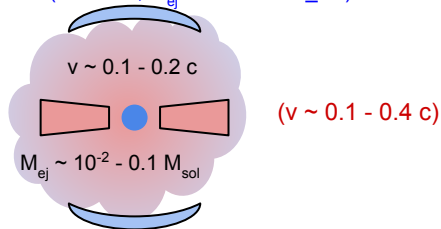
The **chirp mass** provides a strong constraint on the component masses for a given mass ratio:

$$\mathcal{M} = \frac{(M_1 M_2)^{3/5}}{(M_1 + M_2)^{1/5}} = M_2 \frac{q^{3/5}}{(1 + q)^{1/5}}$$

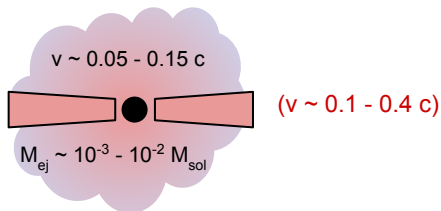
Ejecta in the path of the jet

NS + NS

Fast tail ($v > 0.6 c$; $M_{ej} \sim 10^{-6} - 10^{-5} M_{sol}$)



NS + BH



Before the compact remnant collapses to a BH, the external medium is polluted with ejecta from different channels: (see review by Nakar '19)

- **Dynamical ejecta** ($t < t_{dyn} \sim 10$ ms):
 - **Tidal tails** (equatorial plane)
 - **shock-driven ejecta** (\sim isotropic) - **only in NS+NS merger**
 - Depends strongly on EOS and mass ratio
- **Secular ejecta** ($t > t_{dyn}$):
 - **neutrino-driven wind**
 - **MHD-viscosity-driven wind**

The ejecta expands homologously with density and radial velocity profile:

$$\rho_{ej}(r < R_{ej}, t) \propto \frac{M_{ej}(t)}{R_{ej}^3(t)} \left[\frac{r}{R_{ej}(t)} \right]^{-k}, \quad (k < 3) \quad R_{ej} = \beta_{max} c t$$

$$\beta_{ej}(r < R_{ej}, t) = \beta_{max} \left(\frac{r}{R_{ej}(t)} \right)$$

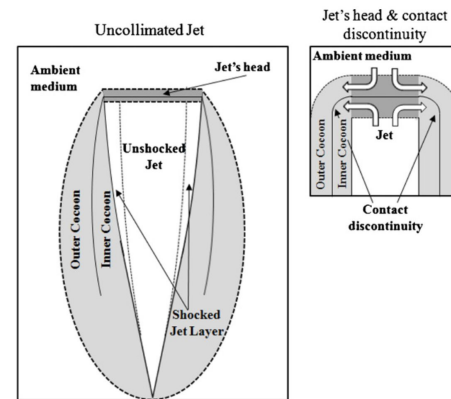
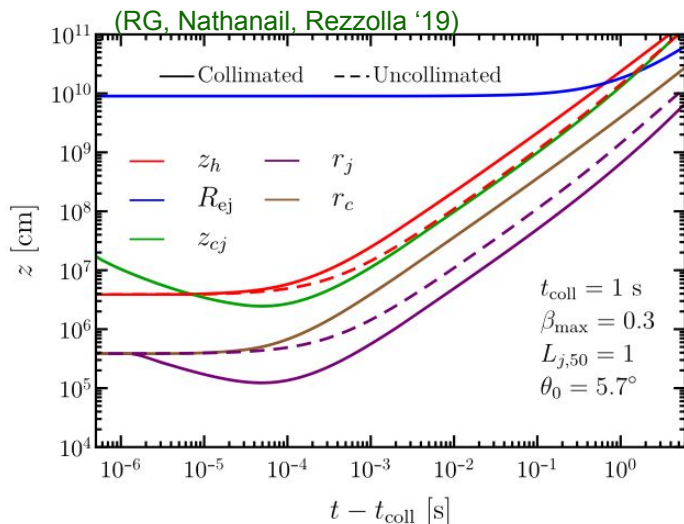
Jet breakout time

The relativistic jet is slowed down by the confining medium. It inflates a cocoon that collimates it.

(Matzner '03; Bromberg+11; Murguia-Berthier+14; Matsumoto & Kimura '18; Lazzati & Perna '19)

$$\beta_h = \frac{\beta_j + \tilde{L}^{-1/2} \beta_{ej}}{1 + \tilde{L}^{-1/2}}$$

$$\tilde{L} \simeq \frac{L_j}{\Sigma_j \rho_{ej} c^3}$$



(Bromberg+2011)

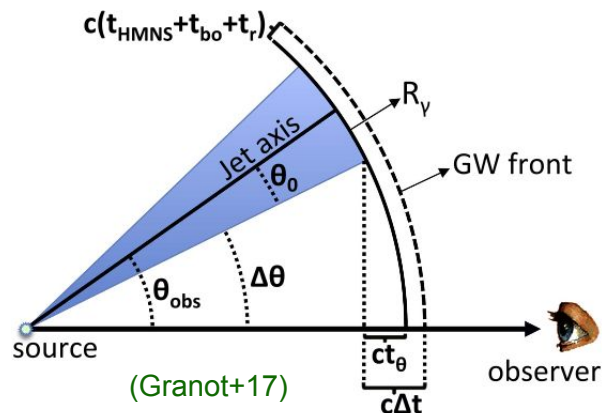
More detailed and simulation calibrated analytic works find some differences with this simple treatment:

(Lyutikov '20; Margalit+18; Hamidani+20; Hamidani & Ioka '21; Gottlieb & Nakar '22;)

Jet breakout time inferred from the plateaus seen in the duration distribution of short GRBs suggests: (Moharana & Piran '17)

$$t_{\text{bo}} \sim 0.4 \text{ s}$$

Radial and angular time delay



Additional time delay is caused by the slower than light expansion speed of the jet and light travel time effects:

Radial delay: $t_R \simeq \frac{R_\gamma}{2\Gamma^2 c} = 1.7 R_{\gamma,13} \Gamma_{2.5}^{-2} \text{ ms}$

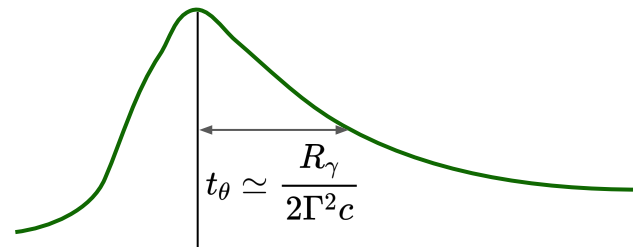
Angular delay: $t_\theta = \frac{R_\gamma}{c} [1 - \cos \Delta\theta] \simeq \frac{R_\gamma}{2c} (\Delta\theta)^2 = 1.67 R_{\gamma,13} \Delta\theta_{-1}^2 \text{ s}$

Total delay: $t_\gamma = t_R + t_\theta \simeq \frac{R_\gamma}{2c} \left[\frac{1}{\Gamma^2} + (\Delta\theta)^2 \right]$

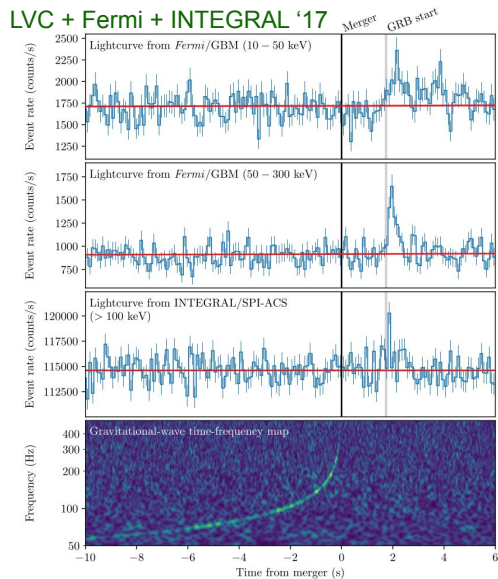
Different emission radii:

- Shock-breakout from fast tail
- Photospheric radius
- Internal shock radius: $R_{\text{IS}} = 2\Gamma^2 c t_v \simeq 6 \times 10^{12} \Gamma_2^2 t_{v,-2} \text{ cm}$

Emission radius from pulse width:



GW170817/GRB 170817A

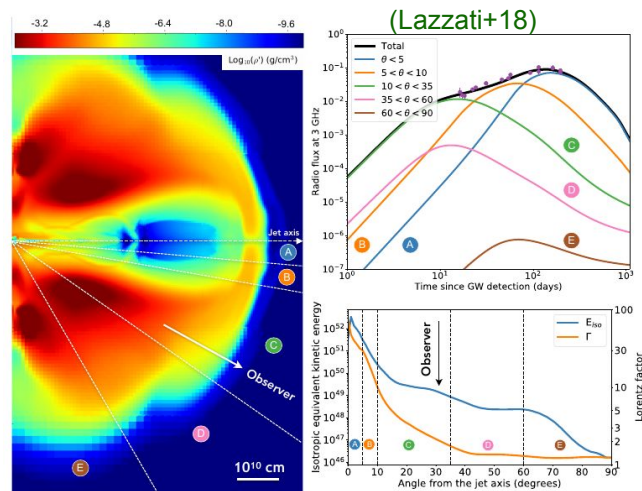


In GW170817, the prompt gamma-ray photons arrived after the GWs with a delay:

$$t_{\text{del}} = 1.74 \pm 0.05 \text{ s}$$

The observer was off-axis ($\theta_{\text{obs}} \sim 20^\circ$) but saw emission from material along the line-of-sight:

- Subluminous prompt emission
- Shallow rise of afterglow lightcurve



Merger remnant did not promptly collapse to a BH:

- $M_{\text{tot}} = 2.74M_{\odot} < M_{\text{th}} = 2.82M_{\odot}$
- Cannot produce “blue” ejecta mass and high electron fraction

Merger remnant collapse time

The delay time was used to constrain the collapse time of the merger remnant:



Model	Δt_{m-j} (s)	η	$\theta_{l.o.s.}$ ($^{\circ}$)	θ_j ($^{\circ}$)
Simulations; baseline ($Y_e = 0.5$; $\Gamma_{l.o.s.} \leq 10$; m_w unconstrained)	<0.36	>240	$23.5^{+5.5}_{-4.5}$	$17.9^{+12.6}_{-3.2}$
Simulations; $\Gamma_{l.o.s.} \leq 7$	<0.18	>240	$24^{+6.9}_{-3.5}$	$18.4^{+12.5}_{-3.1}$
Simulations; $m_w \geq 10^{-2}$	<0.37	>390	$23.6^{+4.8}_{-4.5}$	$17.3^{+13.4}_{-2.3}$
Simulations; $\Gamma_{l.o.s.} \leq 7$; $m_w \geq 10^{-2}$	<0.17	>250	$24.1^{+6.7}_{-3.6}$	$19.3^{+13.9}_{-3.9}$
Parametric; baseline ($Y_e = 0.5$; $\Gamma_{l.o.s.} \leq 10$; m_w unconstrained)	<1.1	>150	$30.3^{+8.5}_{-8.0}$	$10.2^{+8.8}_{-3.0}$
Parametric; $\Gamma_{l.o.s.} \leq 7$	<0.87	>180	$34.4^{+6.4}_{-5.6}$	$9.2^{+9.7}_{-1.8}$
Parametric; $m_w \geq 10^{-2}$	<0.87	>420	$27.5^{+6.0}_{-7.1}$	$16.2^{+11.3}_{-3.2}$
Parametric; $\Gamma_{l.o.s.} \leq 7$; $m_w \geq 10^{-2}$	<0.57	>800	$30.7^{+6.2}_{-6.8}$	$16.3^{+13.8}_{-1.2}$

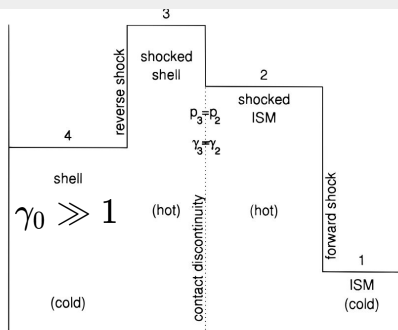


Several works found broadly consistent results, but no strong constraints on the collapse time due to several model uncertainties.

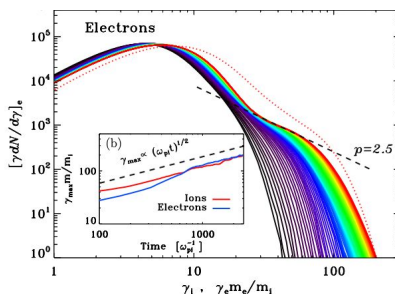
Afterglow Polarization

Afterglow shocks & linear polarization

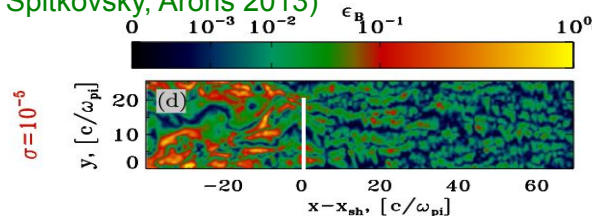
Afterglow shocks are collisionless that accelerate particles into a power-law energy distribution and amplify/generate small-scale B-fields. The particles cool by radiating synchrotron photons.



(Sari, Narayan, Piran 1996)



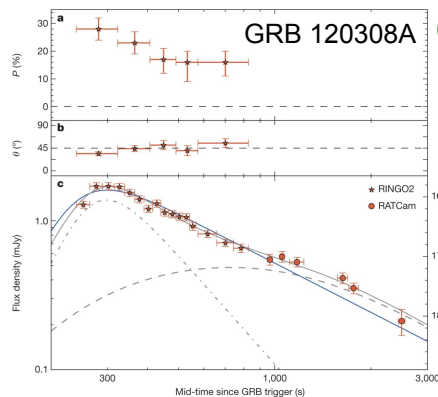
(Sironi, Spitkovsky, Arons 2013)



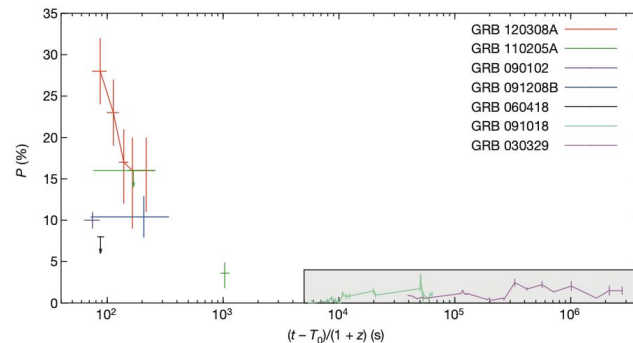
$\sigma = 10^{-6}$

Optical polarimetry of GRB afterglows finds:

- $P \sim \text{few} \times 10\%$ during the **reverse-shock** dominated afterglow (early times)
- $P \sim \text{few} \%$ during the **forward-shock** dominated afterglow (late times)



(Mundell+2013)



Magnetic field structure

B_{\perp} : small-scale ($\Gamma\theta_B \ll 1$) field generated by streaming instabilities;
 - confined to the plane transverse to the shock normal
 (Medvedev & Loeb '99; Gruzinov '99; Sari '99; Granot & Konigle '03)

B_{\parallel} : ordered field aligned along the local shock normal
 (Gruzinov '99; Sari '99; Granot & Konigle '03)

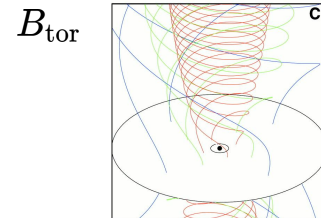
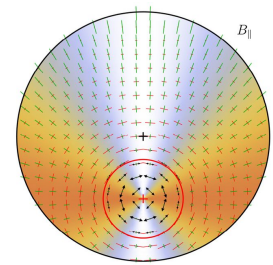
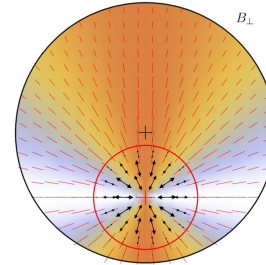
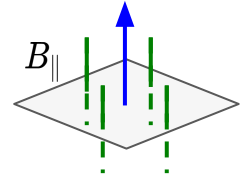
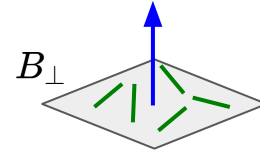
$|P| > 0$ is obtained when symmetry of image is broken:

(a) off-axis observer 'sees' jet edge

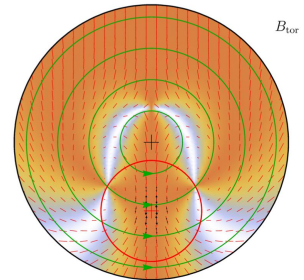
(b) jet angular structure

B_{tor} : globally ordered toroidal field symmetric around the jet axis
 (naturally arises in a high-magnetization outflow)
 (Lyutikov+03; Granot & Taylor '05)

B_{ord} : ordered field within a radiating patch with coherence length larger than the beaming cone: $1/\Gamma \leq \theta_B \ll \theta_j$ (Gruzinov & Waxman '99)



(Meier+01)

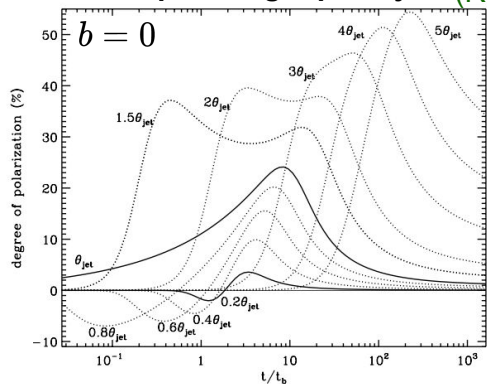


Forward-shock afterglow polarization

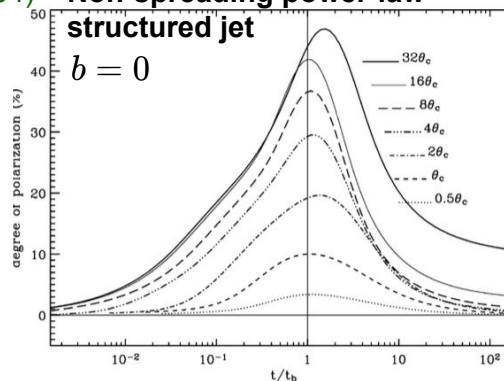
Ignoring the (post-shock) radial structure, polarization is calculated for a prescribed level of B-field anisotropy:
(Gruzinov & Waxman '99; Gruzinov '99; Ghisellini & Lazzati '99; Sari '99; Granot & Konigl '03; Rossi+04)

$$b \equiv \frac{2\langle B_{\parallel}^2 \rangle}{\langle B_{\perp}^2 \rangle} \quad \frac{\Pi_{\text{local}}(\theta')}{\Pi_{\text{max}}} = \frac{(b-1) \sin^2 \theta'}{2 + (b-1) \sin^2 \theta'}$$

Non-spreading top-hat jet (Rossi+04)

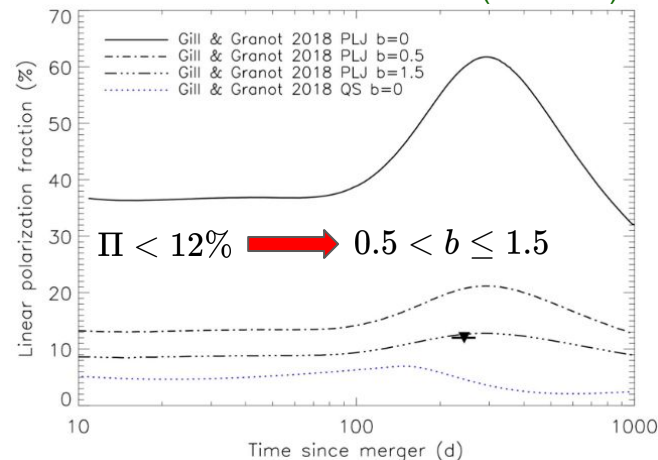


Non-spreading power-law structured jet



Afterglow modeling of GRB 170817A with a power-law structured jet removed the degeneracy!

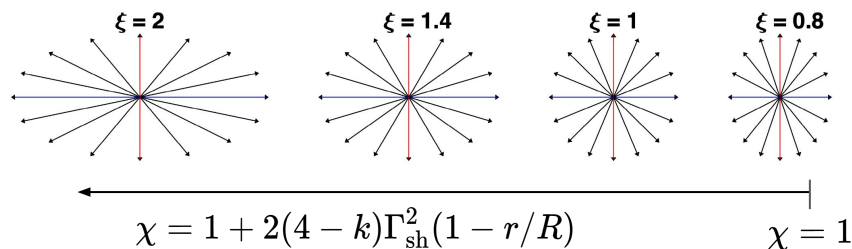
(Corsi+18)



The value of b can only be constrained for a given jet structure and viewing geometry

Constraint on post-shock B-field anisotropy

Including the radial structure of the post-shock flow allows to constrain the B-field anisotropy just behind shock: (RG & Granot 2021)



Post-shock B-field is more isotropic than anisotropic:

$$0.6 \leq \xi_f \leq 0.9$$

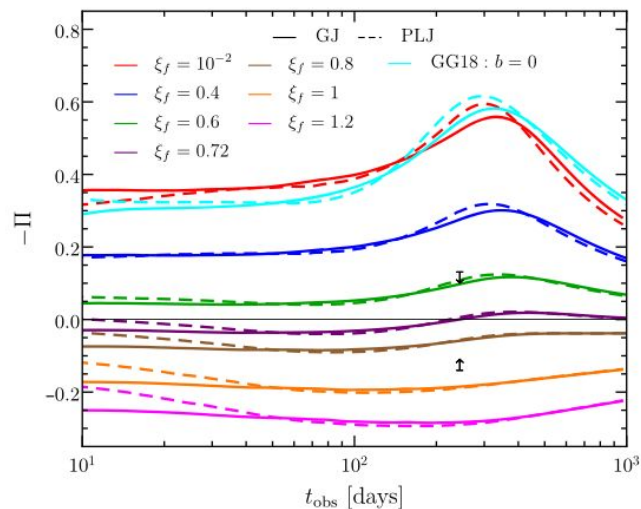
$$0.7 \leq b \leq 1.5$$

(Granot & Konigl '03; Stringer & Lazzati '20)

Macroscopic turbulence at the shock front can yield a more isotropic field (Sironi & Goodman '07; Couch+08; Zhang+09)

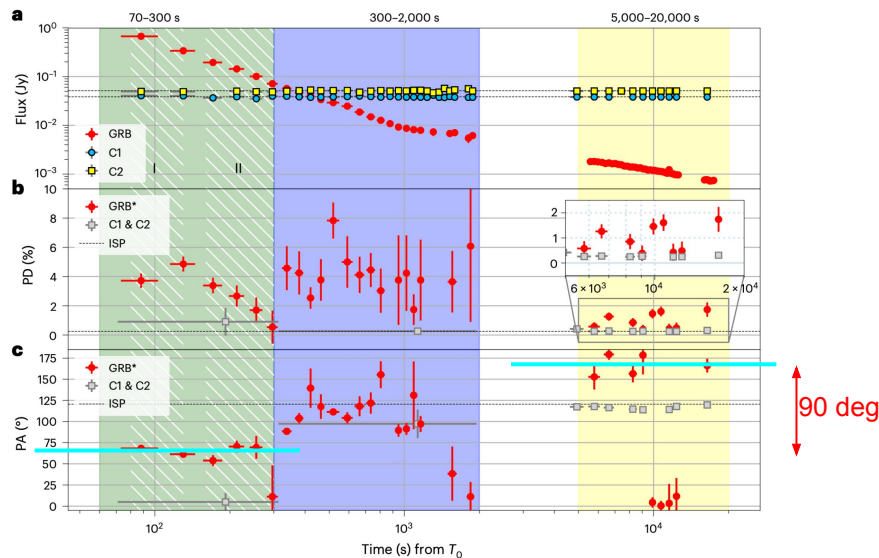
$$\xi(\chi) = \frac{B_{\parallel}(\chi)}{B_{\perp}(\chi)} = \xi_f \chi^{(7-2k)/(8-2k)} \quad n_{\text{ext}} \propto R^{-k}$$

Due to radial stretching of fluid elements, the radial B-field component becomes dominant

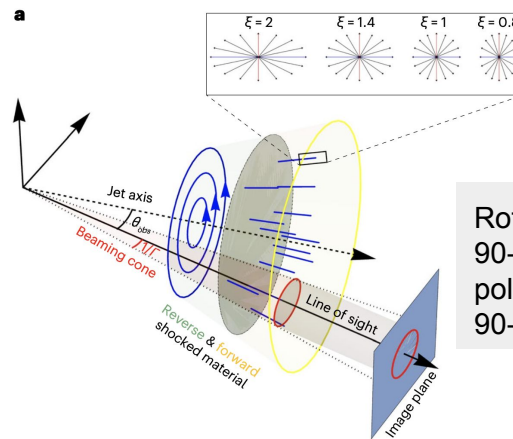
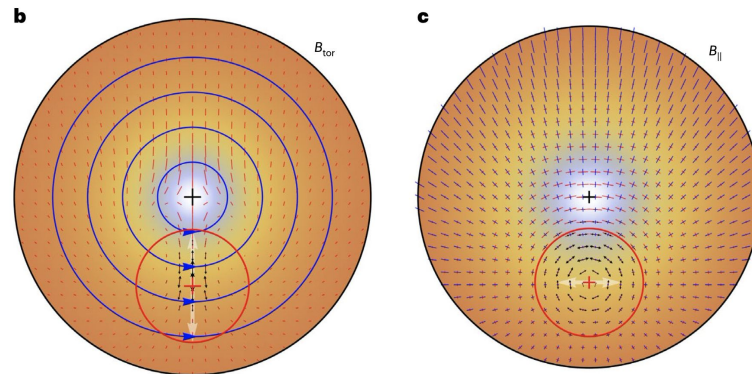


Optical polarimetry of GRB 180720B

(Arimoto+2024)



GRB polarization is obtained after removing any induced polarization en route



$$\hat{\Pi} = \hat{n} \times \hat{B}$$

Rotation of B-field by 90-deg also rotates the polarization vector by 90-deg

Summary & Conclusions

The time delay between reception of GWs and gamma-rays from both long-soft and short-hard GRBs can be instrumental in constraining the **properties of the remnant, jet propagation in the respective confining media, and jet breakout physics**.

There are **still a lot of holes in our understanding jet propagation inside expanding ejecta** and where the gamma-ray emission is generated in jets in short-hard GRBs - shock breakout or internal dissipation?

Afterglow polarization is a valuable tool **for understanding the magnetic field structure in collisionless shocks** and for probing the jet composition.

The prediction of highly anisotropic B-field just behind the shock, which is also obtained in PIC simulations, is at odds with constraints obtained low afterglow polarization measurements, that suggest more mixed B-field components.