

Photometry and elements of GW Geminorum

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Summary. — Photoelectric observations of the eclipsing system GW Gem made during the years 1978 and 1979 enable us to derive nine epochs of minimum light. The period of the binary star appears to be constant. The light curves are analysed referring to the Roche model. The brighter component appears to be an A8 star and the secondary G3-G4 subgiant fills its Roche lobe.

Key words : Eclipsing binary — photometric solutions.

1. Light curves and period. — GW Gem = BD + 27°1494 was discovered to be an Algol-type variable by Hoffmeister (1949). On the basis of photographic material obtained at Sonneberg and Babelsberg Observatories which began in 1928, Löchel (1955) derived several epochs of minimum. Some other photographic epochs have been derived by Kippenhahn (1953) and by Romano and Perissinotto (1968). On the basis of all this material, 48 minima altogether, Romano and Perissinotto calculated the light elements :

$$\text{Min I} = \text{helioc. JD } 2425645.572 + 0.65944354 n .$$

During the following years GW Gem has been monitored assiduously by the Observers of BBSAG (1973-1978) which on the basis of visual measurements calculated 27 epochs of minimum using the tracing paper method. However, as far as we know, no photoelectric light curve has been obtained so far for this relatively bright and short period system.

The observations studied in this article were made through *B* and *V* filters, a Lallemand photomultiplier and a Gardiner type integrator at the 102 cm reflector of the Merate Observatory, during the years 1978 and 1979. The integration time was set to 20 s. The variable was observed differentially relative to the star BD + 28°1494 ; the check star was BD + 27°1497. The extinction coefficients were determined on some nights ; when it was not possible, mean values were used. The extinction corrections exceptionally came out to 0^m005 for *B* and *V* measurements, but for the most part they were quite negligible.

At first sight the brightness of the comparison relative to the check star appeared to be constant. A total of 56 *B* and 54 *V* differential magnitudes $m_{\text{comp}} - m_{\text{check}}$ gave indeed :

$$\Delta B = -0^m.285 \pm .001,$$

$$\Delta V = -0^m.018 \pm .001 \text{ m.e.}$$

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The corresponding standard deviations for a single Δm , 0^m010 and 0^m009 respectively in *B* and *V* conformed to the usual observing conditions in Merate. However when computing the photometric solutions of GW Gem, the residuals of the observations obtained during some nights showed clearly a small and periodic trend. Since no second check star was used and since the number of observations on GW Gem widely exceeds the number of Δm between the comparison and check star, the observations of GW Gem itself better support the variability of BD + 28°1494. Effectively, after comparing both with GW Gem, cleared from the eclipse effects, and with BD + 27°1497, the comparison star turned out to be a δ Scuti star with an overall amplitude of about 0^m035 at the most (Broglia and Conconi, 1979), but which can also decrease below the noise level of measurements, as we have discussed in a separate paper (Broglia and Conconi, 1981). This fact produced some complications when solving the light curves, as will be said in the next section.

The reference star was tied to the standard *UBV* system on three nights. We obtained :

$$\text{BD} + 28^{\circ}1494 : \quad V = 9^m.32 \quad B-V = +0^m.21 .$$

The *V* value refers to the mean brightness of BD + 28°1494. Taking into account the δ Scuti variation, its incertitude is evaluated at 0^m02 at the most, whilst the colour is quite correct.

During fourteen nights we obtained altogether for GW Gem 1252 differential magnitudes in *B* and 1272 in *V*, listed in tables I and II. By fitting a second degree parabola to the lower part of each minimum we derived five epochs of primary and four of secondary eclipse, listed in table III. The quoted errors relate to the mean of *B* and *V* values. Taking into account only the primary minima we calculated the following ephemeris :

$$\text{Min I} = \text{helioc. JD } 2425645.5938 + 0.659443504 n \quad (1)$$

$$\pm \quad \quad \quad 5 \quad \quad \quad 17 \text{ m.e.}$$

To detect eventual changes in the period we have considered moreover the photographic and visual timings of light given in the literature from which we calculated the normal epochs given in table III with the corresponding mean errors, to have their precision valued. After weighting conveniently, all the instants of minimum lead to the following ephemeris :

$$\text{Min I} = \text{helioc. JD } 2425645.5798 + 0.659444013 n \\ \pm 40 \quad 146 \text{ m.e.}$$

The residuals O-C are given in table III. The period including all observations over 50 years would be slightly longer than the value determined from photoelectric data alone. Adding a quadratic term to the ephemeris, a reduction of the mean residual of only four percent is obtained, so on the basis of the meagre material available the period of GW Gem can be considered constant.

The observations were put in phase by means of the ephemeris (1). From the light curves given in figure 1 we deduce :

	Max	Min I	Min II
V	10 ^m 485	11 ^m 450	10 ^m 685
B-V	+ 0.27	0.33	0.24

2. Photometric solutions and concluding remarks. — A preliminary analysis of the light curves according to the Russell model was performed by means of the Irwin (1947) differential correction method in order :

- 1) to separate the eclipse changes from the δ Scuti variation ;
- 2) to evaluate the influence on the solutions of the variability of the comparison.

Harmonic analysis of the residual derived in the photometric solutions were performed, separately for each night and colour. The periods and amplitudes, non constant, of the δ Scuti variation are given elsewhere (Broglia and Conconi, 1981). Using these values the single measurements of GW Gem have been corrected afterwards for the Scuti variation of the comparison, limited to the nights when the variation was detected and the clearing out for the δ Scuti effect proved to be significant in comparison with natural dispersion of the observations. About two thirds of the measurements have been corrected and the corresponding reduction factor of the dispersion was 0.75.

The influence on the photometric solutions of the δ Scuti variation appeared to be negligible because its amplitude is small compared with the eclipse changes and in most parts of the mean light curves the fluctuations cancel out. In fact correcting the out of eclipse measurements the standard deviation for a single observation with respect to the Fourier representation decreased from 0^m009 to 0^m007 in B and from 0^m008 to 0^m006 in V. A similar improvement was attained for the measurements during the eclipse. We note moreover that when solving according to the Russell model the $\sin n\theta$ terms resulted quite negligible.

Starting from these preliminary elements, solutions were then calculated by means of the Wilson and Devinney (1971) programmes, updated to 1978. In order to reduce the computing time when operating with the differential corrections programme we make the

following change. According to the Wilson and Devinney notations the flux sorting in the observing direction from each areola in which both stars are subdivided is equal to :

$$\Delta F_\lambda = \cos \gamma \text{ DIGR}^2 \sin \theta \Delta \theta \Delta \phi / \cos \beta .$$

For a given orbital phase the factor $\cos \gamma$, where γ is the angle between the local surface normal and the line of sight, depends only on the « geometrical » parameters (i , q , Ω_1 , Ω_2) ; the limb darkening D depends on these parameters and on the coefficients x_1 and x_2 ; the product $\text{IGR}^2 \sin \theta / \cos \beta$ depends not only on the geometrical parameters but also on the « photometric » ones (g_1 , g_2 , T_1 , T_2 , L_1 , L_2 , A_1 , A_2 , x_1 , x_2), but not on the phase ; $\Delta \theta$ and $\Delta \phi$ depend on the grid's numbers. In the original programme the quantity $\text{IGR}^2 \sin \theta / \cos \beta$ is computed for the initial set of parameters and the corresponding vector is memorized. Then the luminosity l is computed for each phase by means of the subroutine « Light ». If we want to compute the differential corrections for n parameters we must repeat n times this process after having incremented successively each of the n parameters. On the whole $n + 1$ light curves are computed and from these the derivatives $\delta l / \delta p$ belonging to each of the n parameters p are calculated.

The programme can be improved by storing in a matrix the factor $\text{IGR}^2 \sin \theta / \cos \beta$ computed for the initial set of parameters and for the n sets obtained by increasing by Δp , one after another, each of the n photometric parameters to be corrected. In this way the quantity $\cos \gamma$, corresponding to a given phase and to a given areola, can be computed in the subroutine « Light » only once for all the photometric parameters and we can derive simultaneously for each observation the ΔF_λ pertinent to all the sets of photometric parameters (the initial and the increased ones).

In the case of grids 25×25 and 15×15 , when correcting three photometric and three geometric parameters the computing time is reduced by 30 percent. This improvement is appreciable especially when using a small computer.

Because no spectroscopic study of GW Gem is as yet available in the literature, taking into account the fact that the eclipses are deep, in conformity with the colour at the Min II a spectral type A8 was attributed to the primary component, supposed to be a main sequence star and a temperature $T_h = 7700$ K was assumed according to the Flower (1977) temperature scale. The following parameters were allowed to vary : i , L_1 , L_2 , A_2 , Ω_1 , Ω_2 . Of the remaining parameters which were not adjusted during the calculations, the limb darkening coefficients were taken from Grygar *et al.* (1972), and the gravity darkening exponents were set equal to one for both stars. Since the spectroscopic mass-ratio q is unknown and the solutions show a correlation between q and i , we searched for solutions, by means of the differential corrections programme, with different assumed values for q ranging from $q = 0.32$ to $q = 0.60$ at convenient steps. In the range from $q = 0.32$ to 0.45 the filling factor $F_2 = \Omega_{\text{int}} / \Omega_2$ for the secondary component is 1.0 and in the interval 0.45 to 0.60 it decreases to 0.985 only ; therefore the secondary component fills its Roche lobe.

The best solution (with the smallest sum of the squares of the residuals) is at $q = 0.43$, as appears from figure 2 where the solutions calculated with F_2 as free parameter (dots) and those derived with $F_2 = 1$ (circles) are represented. The adopted solution calculated assuming q also as free parameter and using the programme in mode 0, according to Wilson' code, is listed in table IV together with the related standard errors pertinent to the adjusted parameters. The luminosity of the bright star is normalized to make the sum of the two components unity. The temperature $T_c = 5\,270$ K, calculated according to the Planck's law for the secondary component, favours a spectral type G3-4 for the secondary subgiant. The solutions were calculated using all the B and V individual observations together.

A more realistic evaluation of the uncertainty of the solutions and in particular of the mass-ratio q can be

derived by looking at figure 2. Assuming a 5 percent worsening of the factor R (see legend to figure 2) is significant, an incertitude of ± 0.05 can be assigned to q . The corresponding errors for the elements i , Ω_1 , A_2 , L_{1B} , L_{1V} are given between brackets in table IV.

In conclusion GW Gem appears to be a semidetached system ; the small value for the r.m.s. residual σ for single B or V observations computed in the solution (table IV) and the small dispersion of the measurements displayed in figure 1 confirms that the light curves have been stable and devoid of sensible perturbations over the two observing seasons and that the computed elements are reliable.

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References

- BBSAG Observers : *BBSAG Bull.* n° 8, n° 9, n° 11 (1973) ; n° 13, n° 14 (1974) ; n° 19, n° 20, n° 21, n° 22 (1975) ; n° 26, n° 27 (1976) ; n° 31, n° 33 (1977) ; n° 36 (1978).
 BROGLIA, P., CONCONI, P. : 1979, *Inf. Bull. Var. Stars* n° 1595.
 BROGLIA, P., CONCONI, P. : 1981, *Astron. Astrophys.* **100**, 201.
 FLOWER, P. J. : 1977, *Astron. Astrophys.* **54**, 31.
 GRYGAR, J., COOPER, M. L., JURKEVICH, I. : *Bull. Astron. Inst. Czech.* **23**, 147.
 HOFFMEISTER, C. : 1949, *Erg. Astron. Nachr.* **12**, 1.
 IRWIN, J. B. : 1947, *Astrophys. J.* **106**, 391.
 KIPPENHAHN, R. : 1953, *Astron. Nachr.* **281**, 156.
 LÖCHEL, K. : 1955, *Astron. Nachr.* **281**, 156.
 ROMANO, G., PERISSINOTTO, M. : 1968, *Mem. Soc. Astron. Ital.* **39**, 430.
 WILSON, R. E., DEVINNEY, E. J. : 1971, *Astrophys. J.* **166**, 605.

TABLE I. — *B* observations of GW Gem.

HEL. J.D. 2443..	B												
514.4885	10.933	514.5921	10.918	543.3744	10.747	543.4578	10.811	543.5316	11.514	595.3757	10.835	596.3972	10.814
4829	10.976	5097	10.905	5204	10.742	5402	10.804	5453	11.585	5973	10.836	5987	10.744
4851	11.001	5975	10.878	3774	10.750	4412	10.805	5353	11.585	5983	10.836	5988	10.775
4875	11.020	5998	10.875	3799	10.766	4466	10.802	5357	11.602	5970	10.823	4079	10.789
4907	11.048	6025	10.861	3810	10.757	4456	10.802	5378	11.640	5907	10.822	4130	10.761
4940	11.051	6031	10.859	3833	10.742	4456	10.802	5378	11.640	5908	10.822	845	10.761
4962	11.119	6071	10.849	3841	10.752	4718	10.823	5396	11.652	5851	10.825	4518	10.808
4989	11.191	6104	10.849	3888	10.773	4745	10.809	5413	11.715	5879	10.814	4533	10.793
5038	11.271	6140	10.809	3910	10.755	4768	10.827	5420	11.721	5892	10.809	4554	10.796
5063	11.340	6195	10.808	3936	10.754	4813	10.849	5448	11.761	5923	10.808	4583	10.794
5088	11.356	6220	10.816	3943	10.757	4821	10.850	5456	11.763	5939	10.802	4602	10.836
5111	11.414	6224	10.817	3965	10.754	4841	10.847	5463	11.774	5953	10.815	4622	10.842
5139	11.419	6244	10.817	3977	10.755	4856	10.847	5471	11.775	5974	10.805	4640	10.846
5143	11.458	6291	10.801	3992	10.752	4872	10.890	5501	11.791	5985	10.805	4659	10.857
5163	11.507	543.3217	10.774	4011	10.751	4892	10.890	5519	11.771	4009	10.793	4681	10.878
5184	11.564	3235	10.778	4032	10.752	4900	10.912	5527	11.778	4022	10.796	4689	10.873
5207	11.578	3237	10.778	4035	10.759	4903	10.919	5535	11.783	4035	10.796	4697	10.886
5252	11.702	3271	10.770	4077	10.746	4935	10.923	5555	11.752	4070	10.794	4717	10.889
5275	11.714	3296	10.779	4085	10.751	4945	10.928	5562	11.727	4096	10.777	4738	10.917
5296	11.744	3312	10.773	4124	10.750	4970	10.953	5571	11.724	4115	10.788	4754	10.924
5305	11.751	3317	10.771	4131	10.751	4974	10.944	5579	11.724	4140	10.787	4763	10.924
5360	11.785	3349	10.776	4151	10.754	4997	10.980	5607	11.674	4153	10.791	4780	10.924
5385	11.785	3371	10.774	4158	10.748	5018	11.003	5626	11.627	4187	10.786	4803	10.967
5404	11.808	3388	10.789	4180	10.747	5025	11.015	5643	11.597	4209	10.785	4803	10.995
5425	11.813	3404	10.788	4186	10.747	5032	11.013	5648	11.598	4229	10.785	4803	10.997
5509	11.934	3433	10.774	4243	10.759	5052	11.045	5668	11.644	4334	10.910	4848	10.997
5550	11.945	3436	10.767	4248	10.761	5073	11.081	5678	11.516	4354	10.910	4848	10.997
5581	11.946	3467	10.759	4269	10.750	5081	11.079	5670	11.485	4365	10.901	4869	10.997
5599	11.950	3480	10.750	4270	10.750	5091	11.079	5670	11.485	4378	10.901	4878	10.997
5622	11.301	3517	10.767	4333	10.745	5111	11.129	5717	11.444	4396	10.777	4738	10.917
5641	11.244	3538	10.764	4362	10.769	5146	11.194	5738	11.420	4415	10.788	4754	10.924
5675	11.214	3545	10.765	4369	10.767	5154	11.204	5747	11.377	4430	10.787	4763	10.924
5683	11.214	3547	10.765	4371	10.767	5154	11.204	5756	11.355	4435	10.789	4773	10.924
5714	11.146	3576	10.758	4398	10.789	5184	11.254	5776	11.358	4450	10.786	4783	10.924
5738	11.094	3598	10.769	4429	10.784	5205	11.299	5785	11.299	4464	10.786	4804	10.930
5743	11.101	3623	10.766	4436	10.772	5227	11.325	5803	11.267	4479	10.786	4811	10.930
5822	11.020	3645	10.760	4453	10.772	5234	11.345	5816	11.268	4488	10.786	4818	10.930
5828	11.005	3663	10.756	4492	10.798	5262	11.397	5842	11.203	4495	10.786	4828	10.930
5851	10.979	3688	10.755	4512	10.799	5270	11.416	5851	11.191	4512	10.786	4838	10.930
5869	10.940	3711	10.771	4535	10.805	5297	11.454	5871	11.162	4529	10.786	4848	10.930
5899	10.941	3736	10.774	4555	10.808	5308	11.486	5881	11.150	4540	10.786	4854	10.930

HEL. J.D. 2443..	B												
543.5892	11.433	344.3109	10.771	344.3033	10.763	344.4165	10.822	344.5071	10.795	377.2993	10.795	905.3597	11.314
5900	11.125	3220	10.776	3952	10.751	4644	10.821	5103	10.794	5954	11.330	5116	10.788
5909	11.103	3222	10.772	3976	10.761	4689	10.831	5303	10.794	5989	11.289	5138	10.794
5932	11.074	3243	10.770	4005	10.756	4696	10.822	5360	10.782	5956	11.278	5159	10.784
5941	11.043	3263	10.770	4013	10.755	4717	10.821	5369	10.781	5964	11.270	5169	10.783
5952	11.018	3335	10.768	4042	10.759	4730	10.840	5398	10.793	5973	10.805	5187	10.800
5972	11.018	3335	10.768	4042	10.766	4749	10.825	5316	10.784	6000	10.800	5203	10.824
5982	11.018	3336	10.768	4042	10.766	4749	10.825	5316	10.784	6003	10.800	5222	10.824
6020	11.068	3352	10.769	4065	10.766	4747	10.821	5328	10.784	6014	10.800	5234	10.824
6049	10.934	3392	10.762	4100	10.767	4831	10.828	5340	10.760	6044	10.799	5271	10.811
6059	11.020	3455	10.760	4167	10.782	5254	10.833	5383	10.722	6054	10.799	5277	10.817
6078	11.020	3456	10.760	4167	10.782	5254	10.833	5383	10.722	6055	10.799	5277	10.817
6099	10.896	3442	10.756	4146	10.776	4867	10.837	5393	10.752	6070	10.799	5313	10.854
6119	10.892	3450	10.773	4153	10.771	4887	10.854	5363	10.769	6072	10.799	5334	10.854
6128	10.876	3450	10.770	4176	10.778	4895	10.864	5364	10.774	6073	10.799	5334	10.854
544.2738	10.772	3478	10.758	4207	10.776	5006	10.885	5389	10.762	6074	10.799	5334	10.854
2756	10.848	3502	10.776	4207	10.769	4926	10.840	5364	10.768	6074	10.799	5335	10.854
2774	10.840	3505	10.772	4230	10.770	4946	10.863	5364	10.768	6074	10.799	5347	10.854
2784	10.840	3506	10.772	4230	10.771	4953	10.867	5364	10.768	6074	10.799	5347	10.854
2817	10.827	3567	10.762	4299	10.772	5013	10.873	5376	10.774	6074	10.799	5354	10.854
2825	10.837	3574	10.757	4307	10.776	5040	10.870	5374	10.763	6074	10.799	5354	10.854
2841	10.826	3595	10.758	4329	10.773	5048	10.878	5373	10.760	6075	10.799	5354	10.854
2851	10.807	3795	10.738	5005	10.805	5492	10.917	5394	10.784	6076	10.799	5354	10.854
3060	10.819	3816	10.743	5233	10.800	5490	10.920	5393	10.784	6077	10.799	5354	10.854
3100	10.791	3844	10.744	5250	10.799	5496	10.926	5398	10.785	6078	10.799	5354	10.854
3110	10.791	3844	10.745	5252	10.810	5584	10.920	5399	10.765	6079	10.799	5354	10.854
3118	10.797	3851	10.743	5263	10.807	5365	10.858	5399	10.902	6080	10.799	5354	10.854
3126	10.791	3873	10.743	5213	10.818	5202	10.889	5407	10.783	6081	10.799	5354	10.854
3134	10.781	3873	10.743	5213	10.818	5202	10.889	5407	10.783	6082	10.799	5354	10.854
3140	10.818	3647	10.843	5209	10.807	5323	10.855	5427	10.787	6083	1		

PHOTOMETRY AND ELEMENTS OF GW GEMINORUM

TABLE II. — *V* observations of GW Gem.

HEL. J.D. 2433..	V	HEL. J.D. 2443..	V																
514,4799	10.668	514,6184	10.539	543,3968	10.480	543,4785	10.551	543,5431	11.398	595,3515	10.612	596,3738	10.578	849,4935	10.849	876,3984	10.495	876,4779	10.538
10,683	10.697	10,736	10.529	3995	10.480	4825	10.567	4660	11.441	3522	10.612	3625	10.577	4964	10.885	4021	10.491	4831	10.544
4,4781	10,751	543,3214	10,508	3995	10.480	4825	10.567	4660	11.441	3522	10.612	3625	10.577	4964	10.885	4021	10.491	4831	10.544
4,879	10,755	.3231	10,515	.4014	10,472	4849	10,579	5467	11,443	3547	10,608	3782	10,557	4968	10,896	4028	10,489	4907	10,549
4,908	10,775	.3257	10,501	4035	10,478	4867	10,583	5488	11,444	3546	10,609	3802	10,562	5046	11,018	4053	10,487	4914	10,555
4,938	10,821	.3267	10,496	4036	10,479	4867	10,581	5488	11,444	3547	10,610	3822	10,553	5046	11,022	4053	10,487	4914	10,555
4,985	10,886	.3309	10,511	.4089	10,491	4904	10,621	5523	11,427	3601	10,596	3858	10,540	5093	11,100	4092	10,488	4968	10,567
.5018	10,944	.3334	10,492	.4128	10,487	4926	10,638	5531	11,418	3619	10,603	3866	10,540	5140	11,192	4119	10,481	4985	10,578
.5042	10,947	.3336	10,493	.4136	10,488	4926	10,638	5531	11,418	3620	10,603	3867	10,541	5141	11,190	4120	10,481	4986	10,578
.5051	10,941	.3367	10,500	.4154	10,491	4948	10,659	5559	11,403	3621	10,603	3874	11,373	4159	10,481	4987	10,578		
.5091	11,062	.3385	10,502	.4161	10,487	4974	10,676	5566	11,403	3672	10,592	3969	10,544	5281	11,448	4166	10,481	5088	10,602
.5115	11,105	.3406	10,507	.4183	10,486	4983	10,689	5579	11,378	3691	10,576	4004	10,522	5321	11,475	4190	10,493	5146	10,653
.5122	11,117	.3409	10,502	.4192	10,487	4987	10,691	5581	11,378	3692	10,576	4024	10,522	5321	11,475	4190	10,493	5146	10,653
.5155	11,202	.3452	10,512	.4226	10,500	5014	10,734	5641	11,318	3722	10,572	4088	10,521	5407	11,389	4221	10,508	5175	10,695
.5167	11,204	.3459	10,508	.4245	10,502	5021	10,730	5610	11,282	3754	10,574	4156	10,523	5443	11,323	4228	10,494	5182	10,703
.5188	11,254	.3492	10,494	.4265	10,497	5042	10,751	5646	11,285	3760	10,564	849,4510	10,539	876,3396	10,520	4252	10,508	5206	10,725
.5210	11,283	.3502	10,495	.4274	10,498	5046	10,751	5653	11,285	3761	10,563	4254	10,521	5453	11,323	4258	10,508	5206	10,725
.5214	11,284	.3542	10,489	.4301	10,504	5078	10,800	5671	11,226	3786	10,564	4254	10,521	5453	11,323	4258	10,508	5206	10,725
.5278	11,339	.3549	10,487	.4323	10,513	5085	10,809	5682	11,202	3804	10,561	4557	10,551	5483	10,513	4305	10,502	5263	10,799
.5302	11,412	.3567	10,485	.4330	10,496	5107	10,844	5706	11,141	3824	10,562	4557	10,549	5499	10,519	4330	10,501	5268	10,817
.5333	11,451	.3579	10,486	.4345	10,497	5117	10,853	5713	11,143	3844	10,562	4557	10,549	5502	10,519	4330	10,501	5268	10,817
.5341	11,462	.3582	10,482	.4370	10,507	5139	10,888	5724	11,108	3876	10,562	4557	10,549	5505	10,519	4333	10,502	5268	10,822
.5382	11,443	.3626	10,489	.4393	10,511	5145	10,911	5742	11,085	3889	10,538	4625	10,562	5558	10,506	4368	10,492	5351	10,924
.5425	11,391	.3636	10,483	.4402	10,503	5159	10,915	5752	11,077	3905	10,537	4646	10,566	5565	10,495	4376	10,491	5381	10,998
.5447	11,337	.3639	10,482	.4402	10,502	5162	10,915	5759	11,050	3911	10,538	4646	10,566	5565	10,495	4376	10,491	5381	10,998
.5454	11,338	.3641	10,485	.4439	10,515	5189	10,959	5779	11,032	3924	10,538	4648	10,566	5576	10,495	4376	10,491	5381	10,998
.5536	11,198	.3649	10,482	.4464	10,512	5233	11,040	5788	10,956	3941	10,538	4692	10,610	5597	10,504	4418	10,493	5449	11,086
.5557	11,113	.3715	10,480	.4471	10,524	5239	11,043	5808	10,948	3985	10,536	4713	10,611	5603	10,504	4450	10,490	5472	11,141
.5578	11,081	.3740	10,479	.4470	10,524	5256	11,043	5808	10,948	4080	10,537	4720	10,612	5602	10,504	4450	10,490	5472	11,141
.5581	11,082	.3747	10,479	.4516	10,538	5266	11,049	5838	10,923	4083	10,541	4757	10,551	5483	10,513	4450	10,490	5472	11,141
.5625	11,004	.3769	10,479	.4523	10,538	5274	11,105	5847	10,906	4100	10,541	4757	10,551	5499	10,513	4450	10,490	5472	11,141
.5648	10,967	.3780	10,481	.4582	10,532	5301	11,160	5854	10,896	4148	10,542	4776	10,551	5533	10,513	4450	10,490	5472	11,141
.5672	10,927	.3781	10,478	.4576	10,526	5306	11,160	5864	10,896	4205	10,540	4784	10,551	5533	10,513	4450	10,490	5472	11,141
.5687	10,928	.3784	10,478	.4576	10,526	5313	11,160	5884	10,864	4206	10,540	4787	10,551	5533	10,513	4450	10,490	5472	11,141
.5621	10,737	.3837	10,472	.4643	10,545	5338	11,246	5895	10,845	4230	10,540	4812	10,710	5753	10,492	4457	10,499	5570	11,324
.5858	10,714	.3847	10,469	.4652	10,544	5346	11,245	5910	10,836	4230	10,540	4835	10,727	5760	10,496	4457	10,499	5570	11,324
.5906	10,659	.3871	10,473	.4673	10,540	5349	11,241	5913	10,823	3619	10,647	4852	10,745	5765	10,497	4457	10,499	5570	11,324
.5929	10,653	.3873	10,473	.4682	10,540	5352	11,241	5916	10,823	3620	10,647	4851	10,745	5766	10,497	4457	10,499	5570	11,324
.5983	10,611	.3914	10,474	.4713	10,540	5391	11,335	5945	10,784	3666	10,621	4881	10,780	3921	10,477	4632	10,508	5672	11,440
.6033	10,598	.3921	10,475	.4740	10,549	5399	11,342	5964	10,739	3690	10,610	4888	10,788	3928	10,485	4658	10,513	5679	11,452
.6078	10,580	.3939	10,475	.4749	10,543	5413	11,345	5970	10,737	3710	10,602	4910	10,820	3953	10,479	4672	10,537	5708	11,445
.6137	10,548	.3940	10,476	.4750	10,544	5414	11,344	5970	10,737	3718	10,602	4929	10,820	3953	10,479	4672	10,537	5708	11,445
.6157	10,519	.3870	10,479	.4768	10,539	5704	11,642	5986	10,497	3957	10,701	4978	10,820	3953	10,479	4672	10,537	5708	11,445
.6282	10,556	.3512	10,497	.4227	10,490	4966	10,604	5617	11,673	3972	10,490	4966	10,820	3953	10,479	4672	10,537	5708	11,445
.2848	10,543	.3549	10,493	.4249	10,487	5048	10,630	5638	11,641	3972	10,490	4966	10,820	3953	10,479	4672	10,537	5708	11,445
.3035	10,537	.3736	10,483	.4435	10,501	5506	11,675	5681	10,495	3992	10,997	5204	10,517	5047	10,517	4055	10,582	4442	10,488
.3035	10,537	.3736	10,483	.4435	10,501	5506	11,675	5681	10,495	3992	10,997	5204	10,517	5047	10,517	4055	10,582	4442	10,488
.3041	10,537	.3736	10,483	.4435	10,501	5506	11,675	5681	10,495	3992	10,997	5204	10,517	5047	10,517	4055	10,582	4442	10,488
.3041	10,537	.3736	10,483	.4435	10,501	5506	11,675	5681	10,495	3992	10,997	5204	10,517	5047	10,517	4055	10,582	4442	10,488
.3224	10,501	.3920	10,481	.4631	10,535	5288	10,497	4021	10,490	4087	10,505	5396	10,753	3996	10,522	4442	10,488	4442	10,582
.3232	10,505	.3920	10,481	.4631	10,535	5288	10,497	4021	10,490	4087	10,505	5396	10,753	3996	10,522	4442	10,488	4442	10,582
.3252	10,515	.3929	10,476	.4663	10,534	5304	10,500	4074	10,474	4141	10,509	5428	10,753	3997	10,522	4442	10,488	4442	10,582
.3252	10,515	.3929	10,476	.4663	10,534	530													

TABLE III. — *Times of minima of GW Gem.*

n	helioc. JD	m.e.	O-C	Observer
0	2425645.569	$\pm 0^d.007$	-0 ^d .011	ph (6) L
1131	26391.416	.007	+ .005	ph (13) K
4325	28497.671	.006	- .004	ph (8) L
4514	28622.324	.006	+ .014	ph (7) K
7741	30750.346	.007	+ .010	ph (5) L
16045	36226.348	.011	- .011	ph (5) R,P
20555	39200.426	.003	- .026	ph (4) R,P
24440	41762.390	.002	- .002	v (6) BBSAG
25412	42403.367	.001	- .004	v (8) "
26008	42796.401	.002	+ .001	v (8) "
26474	43103.701	.004	.000	v (5) "
27097	43514.53438	.00003	+ .00011	pe B,C
27141	43543.55006	.00004	+ .00026	pe "
27142.5	43544.5411	.0005	+ .0021	pe "
27192.5	43577.5120	.0004	+ .0008	pe "
27210.5	43589.3798	.0010	- .0014	pe "
27605	43849.53175	.00006	- .00007	pe "
27646	43876.56881	.00006	- .00022	pe "
27690	43905.58451	.00001	- .00006	pe "
27721.5	43926.3566	.0003	- .0004	pe "

L = Löchel (1955); R, P = Romano and Perissinotto (1968).

K = Kippenhahn (1953); BBSAG = BBSAG Observers (1973-1978).

B, C = Broglia and Conconi, present work.

TABLE IV. — *Photometric elements of GW Gem.*

i = 81°.41 ± 0.08 p.e. (1.4)	r _{1,pt} = 0.380	r _{2,pt} = 0.415	g ₁ = 1.00
q = 0.436 ± 0.004 (.05)	r _{1,s} = 0.361	r _{2,s} = 0.302	g ₂ = 1.00
Ω ₁ = 3.271 ± 0.003 (.017)	r _{1,b} = 0.372	r _{2,b} = 0.334	A ₁ = 1.00
Ω ₂ = 2.751 (contact)	r _{1,pl} = 0.350	r _{2,pl} = 0.289	A ₂ = 0.50 ± 0.01 (.03)
λ x ₁ x ₂ L ₁			
0.430 μ	0.78	0.83	0.9283 ± 0.0006 (.007)
0.550	0.60	0.70	0.8936 ± 0.0008 (.008)
			ε = 0 ^m .008

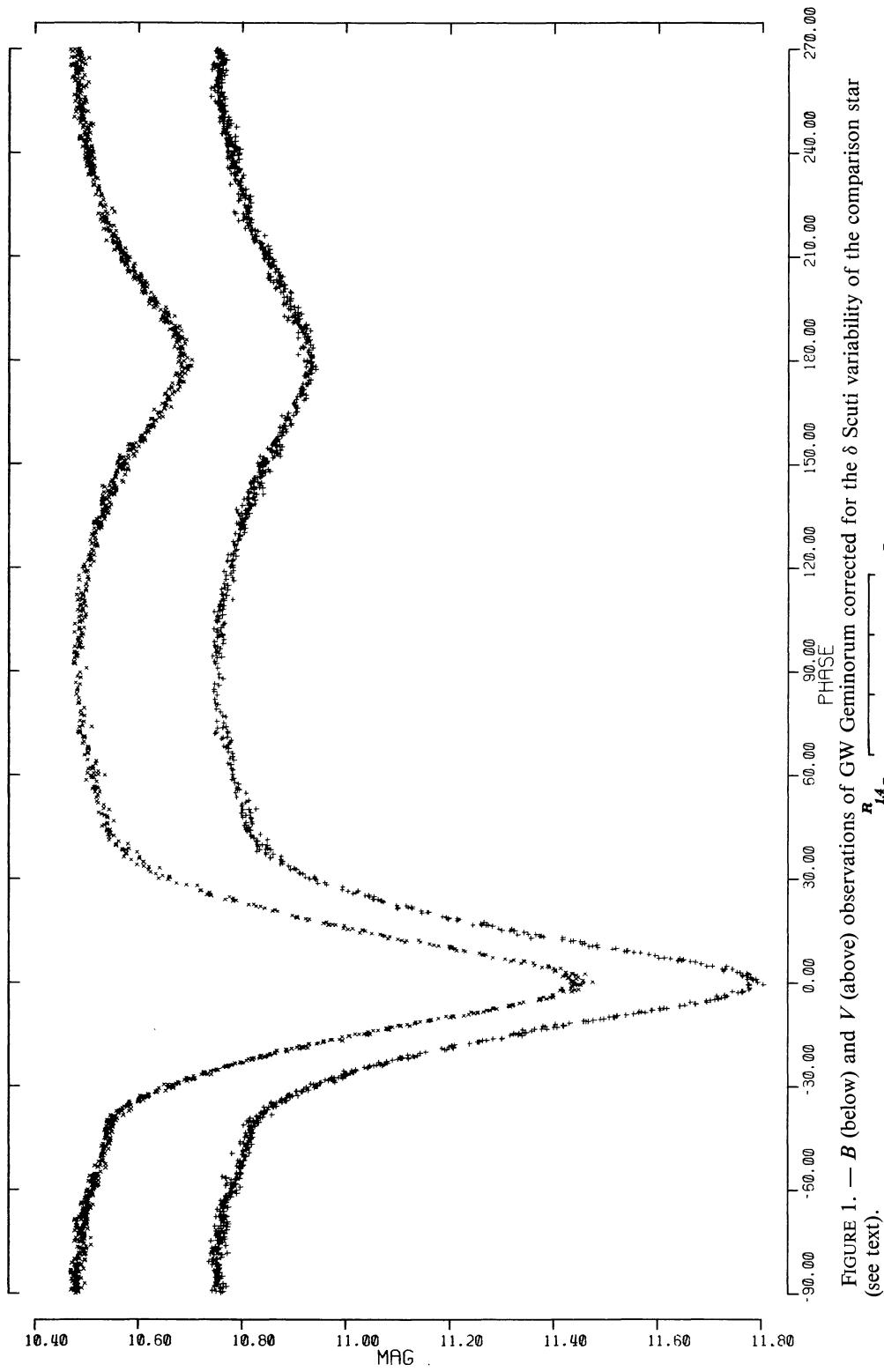


FIGURE 1. — *B* (below) and *V* (above) observations of GW Geminorum corrected for the δ Scuti variability of the comparison star (see text).

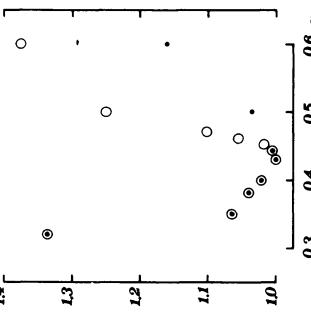


FIGURE 2. — Representation of the solutions calculated with assumed values for the mass ratio q . R is the ratio between the sum of the squares of residuals of a given solution and the corresponding value for the best solution.